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Introduction to Computer Vision

Introduction to Stereo Imaging and the associated project.

Stereo Imaging

The human eyes both take independent “photos” at different angles and positions. The remarkable thing about the human brain is that it is able to use both images to recreate the 3D world. It does this very quickly and remarkably accurately.

To replicate this in computers is a crucial part of image processing and robotics. A computer’s ability to understand its own position compared to its surroundings is a crucial step forward. This would allow the ability for robots to go where humans could not and “learn” useful information about their surroundings.

In the scope of this project we try to replicate basic Stereo Imaging given two photos taken at different horizontal positions from each other. We are going to rebuild the 3D space possible with two images, with depths from the camera plane.

Correspondence Problem

Briefly explains Stereo Imaging using the SIFT algorithm

Correspondance Problem

Stereo Image Matching

Given any two images of the same scene one may want to understand where given parts of the picture exist in the other. Most often is it virtually impossible to take identical picutres with the same scene in exactly the same positions for two or more images.

There are two methods of corresponding two images. The classical method is to analyze a location on an image and see where is it most like on the other image. This is called the **Correlation-Based Method**. The more robust and practical method is the **Feature-Based Method** that indentifies unqiue features in one image and finds the same features in the other image.

A **Feature** is best desribed as a unique piece of the image that is not repeated anywhere else in the picture. There are many methods to indentifying features in a given image, however the method that lent itself well to our partcular problem of replicating stereo imaging is the SIFT Alogrithm.

SIFT Alogrithm

Briefly explains the general SIFT algorithm, pros and cons.

SIFT Alogrithm

Scale Invariant Feature Transform Alogrithm

This algorithm was developed by David Lowe in 1999 at the Univeristy of British Columbia. Through it methodology the **SIFT Alogrithm** is invariant to scale, light, noise and other commons changes that can effect an object's representation in an image. The alogrithm best identifies objects with clear edges, points of high contrast, and stable fundamental geometry that will not change from picture to picture. The features the method displays, not only have their respective x,y corrdinates in the photo, but also have an oriention in radians, and a scale factor to describe the size of the feature. This allows for accurate description of the uniqueness of the feature. All of this lends itself well to solving the correspondance problem presented with two or more images.

Regardless of scale or orientation or position the SIFT alogrith will be able to tell where a particular feature is based on the geometry of the photo and the features nearest to the feature being matched, as well as its descriptors.

SIFT Alogrithm Feature Extraction Example

An example of the characteristics and abilities of feature matching, using SIFT.

Feature Extraction

Application of Feature Extraction

Two images of the same bear on a desk taken at different horitzonal positions relative to the subject were taken and anaylzeed using the SIFT algorithm implemented in Matlab with the aid of a toolbox by VLFeat.

Picture A



Taken on a DSLR Nikon D3000

Picture B



A horizontal shift from camera position in Picture A

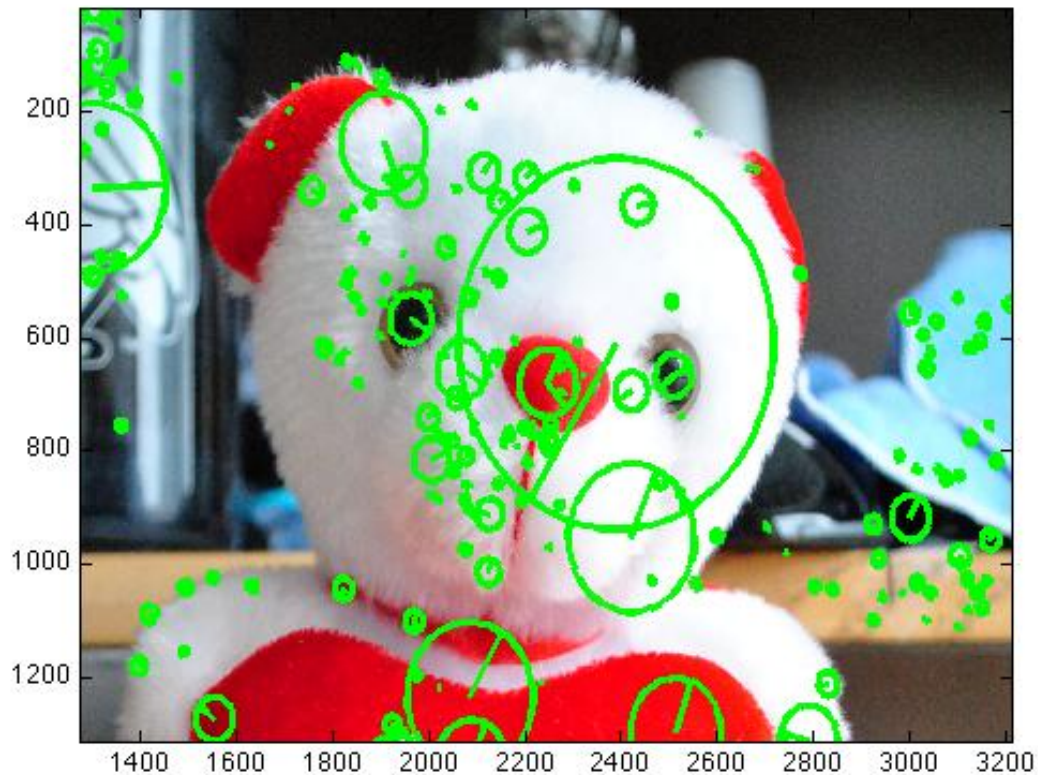
After the SIFT algorithm has been applied corresponding features are very clear and intuitive.

Zoomed In Feature Extraction Picture A



Features(Green) with scale and orientation

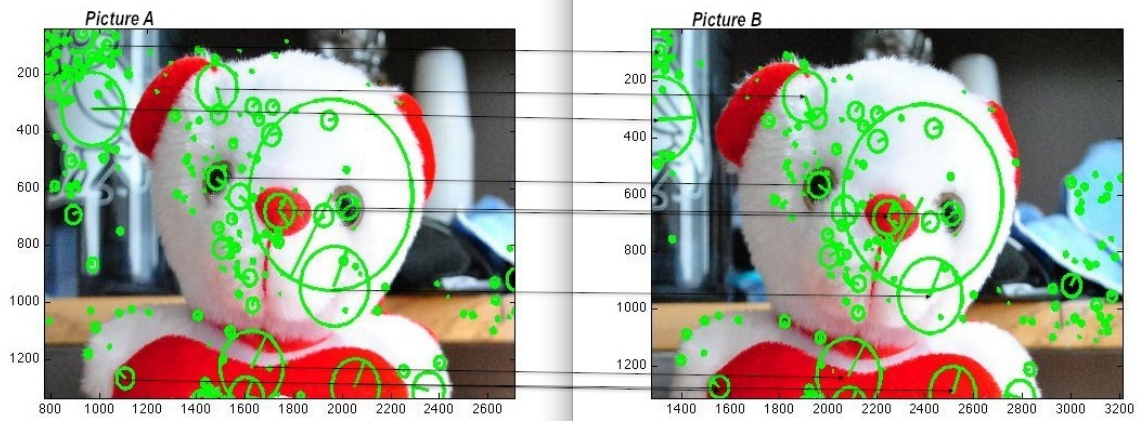
Zoomed In Feature Extraction Picutre B



Features(Green) with scale and orientation

It is clear that the SIFT program chooses the same features of the same scale and orientation in each image, and there is a clear match between the two images.

Matching Features



Black line drawn from center of corresponding features.

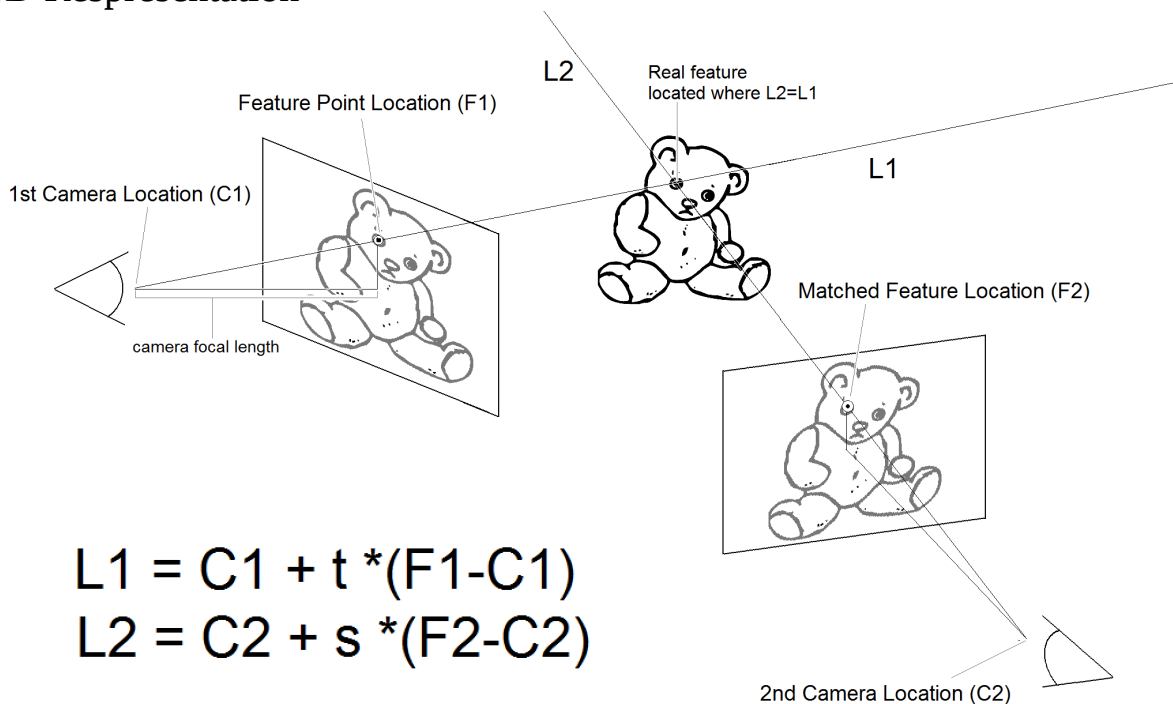
Triangulation

Explains the initial set up, as well as its shortcomings.

Triangulation

Once the SIFT algorithm has been applied, one has positions of corresponding features in each image. To rebuild each point in 3D space, to undo the projection induced by the camera, we represent our camera using the pin hole model. This assumption allows us to draw a line from the camera position to the feature, obtaining an equation for a line that can be used to approximate further points down that line beyond our feature. Obtaining equations for each photo and its respective camera we can build a system of equations to see where these two lines intersect. The position of camera one and camera two are varied by some horizontal distance or **disparity**, similarly as features in photo one and photo two. The figure shows the general idea behind this reconstruction

3D Representation



Bear at two different angles with corresponding feature.

However this is a “perfect” model that inherently has many flaws. One there is going to be a scale problem because we are not sure if we took the picture with a small or big camera of a small or big “world.” This trick can be seen in old movies when you see Godzilla destroying a city, when it is actually a man in a costume jumping on blocks or when a big building is simply a clay miniature shot up close.

The second problem is that this method requires we know the position and the disparity of the cameras before hand to solve this eqation.

Lastly, due to imperfections that will always exist in a photograph, the corresponding features have both vertical and horizontal disparities, not just one or the other, therefore the lines will not truly ever intersect.

Triangulation of Feature Points

Using least squares regression with corresponding feature points and camera position, triangulation can be achieved.

Minimization of Corresponding Feature's Line Equations

Least Squares Method

Granted in our attempt to solve this problem, one knows the **position** and **disparity** of the cameras, our problem becomes a **minimization problem**. Due to the imperfections inherent in photography, the features of one photo will never truly intersect with that of another. So instead of trying to solve for the intersection of two lines, one can perform a **least squares minimization** to see where the two lines in space get closest. Once this value has been obtained, it can be used back into either line equation to find the corresponding point in 3D space. This point with x,y, and z coordinates, z being the distance the point exists away from the camera, now has a proportional depth to that of the camera, and image plane. If this process is done for each corresponding set of features in both images, we arrive at depths of all our feature points from the camera.

Disparities Error

The least squares method is the most realistic. Given the focal length, and positions of the camera the entire world can be recreated, with proportional scale and correct orientation. However, this method in practice is the most unstable, a couple of incorrect matches with the SIFT algorithm can report incorrect depths and throw off a whole region of the depth map. In addition even with the least squares method, if the feature points are incorrect the depth will be wrong. This is why a very high threshold for the SIFT algorithm is desirable to get rid of less correlated matches. Our group would rather have fewer features but be correct, than a lot of features with high error.

In response to this instability, we also plotted proportional depth maps simply using disparities of the camera and the corresponding features to get a sense of the relative depths. This method does not output correct values for Z but is much more stable than potential incorrect least squares method pinpointing.

Depth Maps

Utilizing the SIFT algorithm and Minimization to achieve depths and a depth map.

Depth Map Generation Using SIFT and Minimization Algorithms

Feature Depths to Depth Map

Using the `griddata` and `surf` functions in Matlab, we are able to interpolate the z data of each feature in 3D space, to see what the rest of the regions in between features is doing. Then by laying an original picture over this data we can see visually how deep regions of our photographs are in space.

Given these Two Images:

Picture A



Bear on a desk, with a wall and a deep hallway.

Picture B



Same scene,different camera position.

Applying our least squares algorithm:

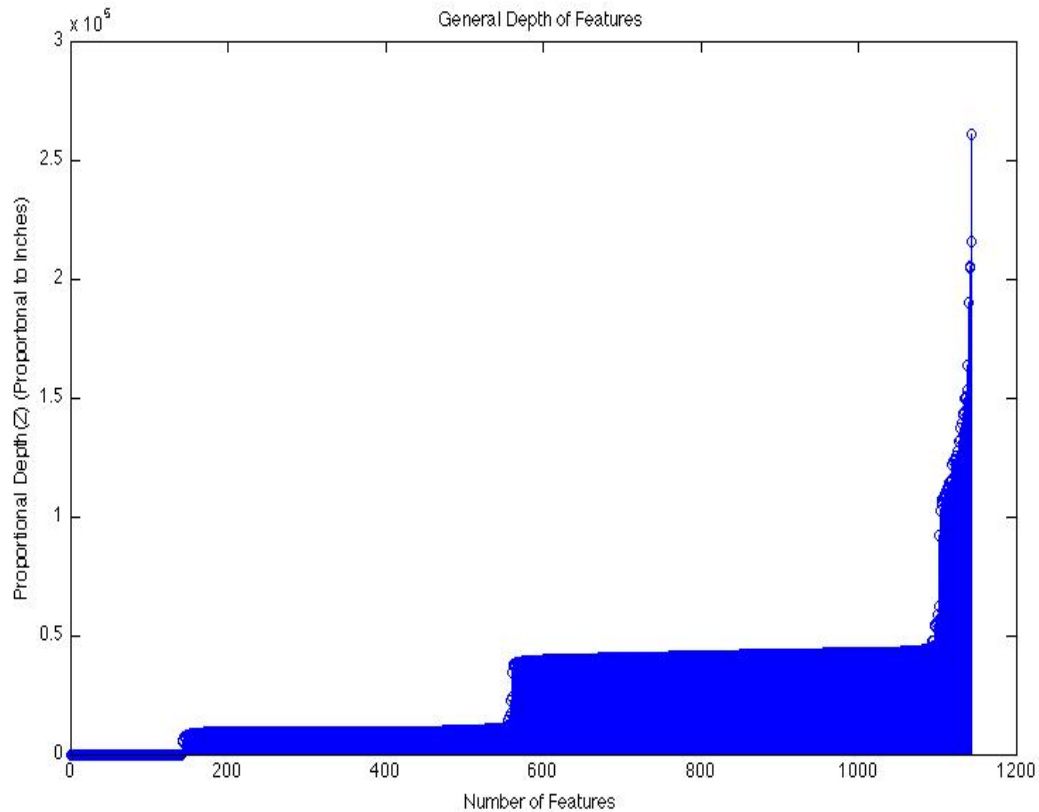
Depth Map with SIFT and Least Squares Minimization



Note: Aside from the extremes in the very front and back left corner, depths make sense. Shallow over bear, deeper to the left with the near by wall, and very deep to the right with the door.

As was mentioned earlier, the least squares method is more unstable and is visibly so with the extremes in the front of the photo and in the back left corner. However the rest of the photo makes intuitive sense. All the reported Z values are off by a scale factor due to the explained ambiguity.

Generalized Range of Depths (proportional to real value in inches)



Note: Region 200 to 600 is the bear's depth, 600 to 1000 is the background(wall), and 1000 to the end is the extreme depth represented by the hallway.

Proportionally this graph makes sense because the wall was in fact about 3 times as far as the bear was to the camera, and the depth of the hallway was obviously extreme compared to the wall because we could not see the end of it in the photo, it seemed to go to infinity.

Therefore these results and the corresponding depth map of the two stereo images fits our expectations.

Depth Map Simply Using Disparities

Depth Map just using Disparities as the Basis



Bear raised, hallway w/ extreme depth

This method is much more stable and demonstrates better quick changes in depth than the previous method. This algorithm understands that there is a huge drop from the depth of the bear to the hallway to the right of it.

Data for this section is not important because all values do not take into consideration 3D space, simply the disparities of the features and the camera positions.

Another Example

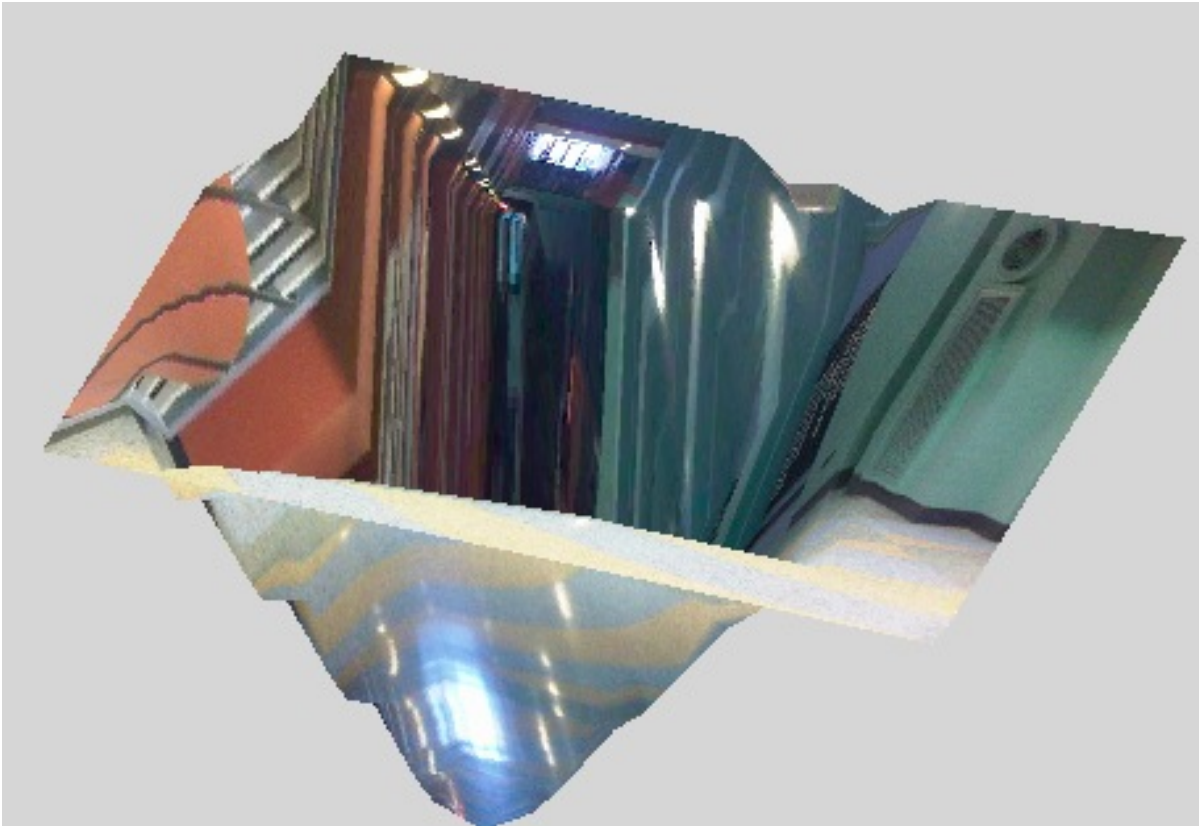
To further test our algorithm on a large depth, we shot two stereo images of the Duncan wall way and used the Disparity method as shown above to get an idea of the relative depths.

Original Photo of Duncan Hall



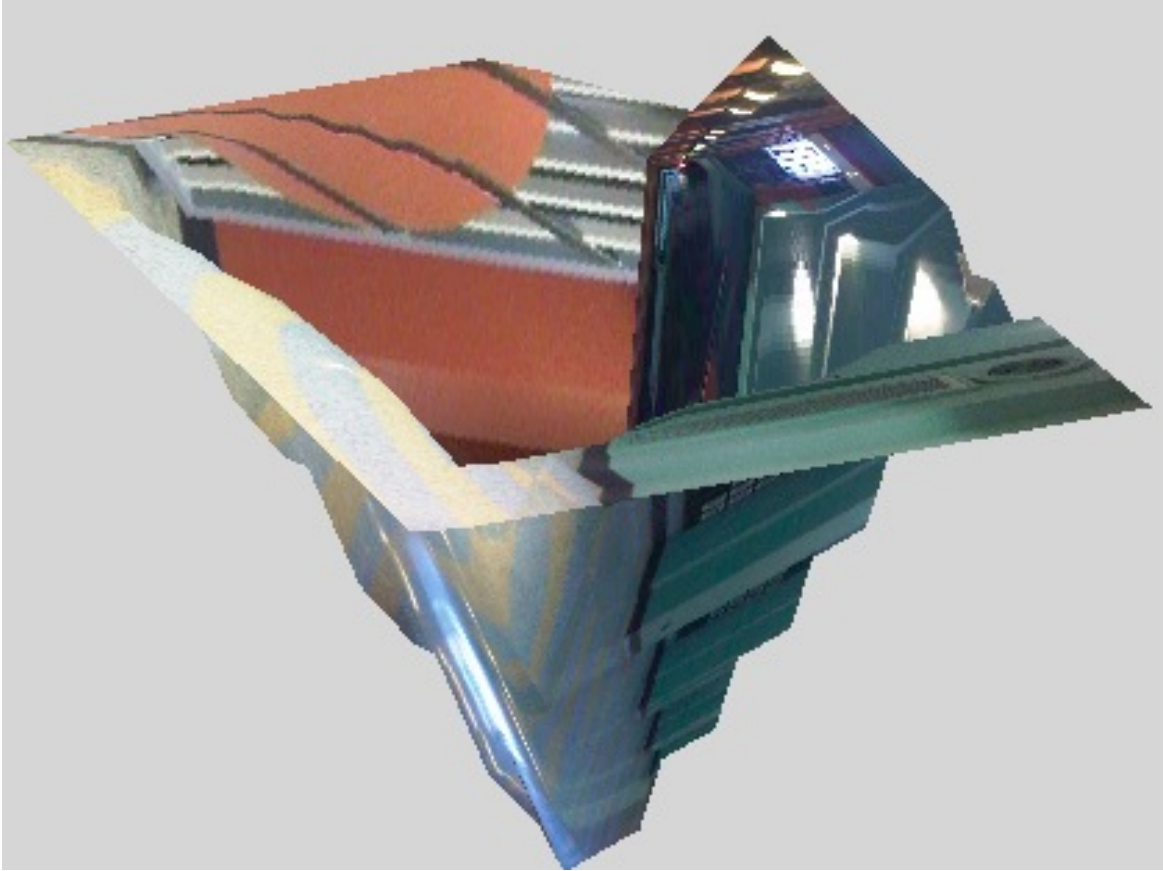
Large Depth w/terminating end,and shallow walls.

Depth Map using Disparites Angle 1



Note: Notice large Depth that terminates correctly where the end of the hall should be.

Depth Map using Disparities Angle 2



Note: Notice how Side Wall Depth is accurate with jagged depths that match the surface of the real walls in Duncan Hall.

Once again we see that this algorithm is very powerful in transforming two stereo images into a depth map, that is also very accurate in its proportional depth from camera.

Conclusion and Acknowledgements

Conclusion

In conclusion replicating Stereo Imaging was a success. We achieved proportional depth maps, that accurately map the 3D space of a scene given two images of the same scene at different angles. Granted there was a lot of control in this experiment the given camera positions and disparities, it was prone to many instabilities. These instabilities did not ruin the depth map, but threw off certain regions that could be accounted for. However when two photos were deliberately taken with terminating ends in view, the algorithm work very well. Future scope of this project would be given many images of the same scene at many different angles and without camera positions we could recreate a complete 3D replication of the scene, object. This could then be used to replicate intricate worlds and scenes with incredible detail.

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